

## A counterexample on the conjecture and bounds on $\chi_{gd}$ -number of Mycielskian of a graph

David A Kalarkop\* and R.Rangarajan†

Department of Studies in Mathematics, University of Mysore,  
Manasagangothri, Mysuru – 570 006, India

\*[david.ak123@gmail.com](mailto:david.ak123@gmail.com)

†[rajra63@gmail.com](mailto:rajra63@gmail.com)

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**Abstract:** A coloring  $C = (V_1, \dots, V_k)$  of  $G$  partitions the vertex set  $V(G)$  into independent sets  $V_i$  which are said to be color classes with respect to the coloring  $C$ . A vertex  $v$  is said to have a dominator (dom) color class in  $C$  if there is color class  $V_i$  such that  $v$  is adjacent to all the vertices of  $V_i$  and  $v$  is said to have an anti-dominator (anti-dom) color class in  $C$  if there is color class  $V_j$  such that  $v$  is not adjacent to any vertex of  $V_j$ . Dominator coloring of  $G$  is a coloring  $C$  of  $G$  such that every vertex has a dom color class. The minimum number of colors required for a dominator coloring of  $G$  is called the dominator chromatic number of  $G$ , denoted by  $\chi_d(G)$ . Global Dominator coloring of  $G$  is a coloring  $C$  of  $G$  such that every vertex has a dom color class and an anti-dom color class. The minimum number of colors required for a global dominator coloring of  $G$  is called the global dominator chromatic number of  $G$ , denoted by  $\chi_{gd}(G)$ . In this paper, we give a counterexample for the conjecture posed in [I. Sahul Hamid, M.Rajeswari, Global dominator coloring of graphs, Discuss. Math. Graph Theory 39 (2019), 325–339] that for a graph  $G$ , if  $\chi_{gd}(G) = 2\chi_d(G)$ , then  $G$  is a complete multipartite graph. We deduce upper and lower bound for the global dominator chromatic number of Mycielskian of the graph  $G$  in terms of dominator chromatic number of  $G$ .

**Keywords:** Global Dominator coloring, global dominator chromatic number, dominator coloring, dominator chromatic number

**AMS Subject classification:** 05C15, 05C69

### 1. Introduction

By a graph  $G = (V, E)$ , we mean a simple graph whose vertex set is  $V$  of order  $n$  and edge set is  $E$  of size  $m$ . For all basic graph theoretic terminologies we refer to [5]. Domination and coloring are two interesting and well known areas in graph theory.

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\* *Corresponding Author*

Domination has rich applications in computer science, communication networks and so on. Graph coloring has applications in scheduling, register allocations, pattern matching and so on (for more details refer to [3]).

A subset  $D$  of the vertex set  $V$  of  $G$  is said to be a dominating set if every vertex of  $V$  is in  $D$  or has a neighbor in  $D$ . The minimum cardinality of a dominating set of  $G$  is called as *domination number* of  $G$ , denoted by  $\gamma(G)$ . A vertex is said to dominate subset  $S$  of  $V(G)$ , if  $v$  is adjacent to all the vertices of  $S$ . For more information on domination, refer to [9]. A coloring of  $G$  is an assignment of colors to the vertices of the graph  $G$  such that no two adjacent vertices receive the same color. The minimum number of colors required for coloring  $G$  is said to be the *chromatic number* of  $G$ , denoted by  $\chi(G)$ . A vertex  $v \in V(G)$  in the coloring  $C = (V_1, \dots, V_k)$  is said to have dom color class  $V_i$  (anti-dom color class  $V_j$ ) if  $v$  is adjacent to all (none) of the vertices of  $V_i$  ( $V_j$ ).

Dominator coloring of  $G$  is the coloring of  $G$  such that every vertex of  $G$  has a dom color class. The minimum number of colors required for dominator coloring of  $G$  is called dominator chromatic number of  $G$ , denoted by  $\chi_d(G)$ . The dominator coloring of  $G$  with minimum number of colors is said to be  $\chi_d$ -coloring of  $G$ . Dominator coloring was studied for the first time by Gera et al. [7]. Global dominator coloring of graphs was introduced by Hamid et al. [11]. Global Dominator coloring of  $G$  is the coloring of  $G$  such that every vertex of  $G$  has a dom color class and an anti-dom color class. The minimum number of colors required for global dominator coloring of  $G$  is called global dominator chromatic number of  $G$ , denoted by  $\chi_{gd}(G)$ . The global dominator coloring of  $G$  with minimum number of colors is said to be  $\chi_{gd}$ -coloring of  $G$ . For good number of results, conjectures and open problems on dominator coloring as well as global dominator coloring of graphs, refer to [2, 7, 8, 10, 11]. The following results are crucial to prove the main results of this paper,

**Theorem 1.** [2] *For any graph  $G$ ,  $\chi_d(G) + 1 \leq \chi_d(\mu(G)) \leq \chi_d(G) + 2$ . Further if there exists a  $\chi_d$ -coloring  $C$  of  $G$  in which every vertex  $v$  dominates a color class  $V_i$  with  $v \notin V_i$ , then  $\chi_d(\mu(G)) = \chi_d(G) + 1$ .*

$N(v) = \{u \in V(G) : uv \in E(G)\}$  and  $N[v] = N(v) \cup \{v\}$  are the open neighborhood and closed neighborhood of the vertex  $v$  of  $G$  respectively. The vertex  $v$  of  $G$  with respect to the coloring  $C$  is said to be solitary if  $\{v\} \in C$  and  $N(v)$  does not contain any color class. Let  $C = (V_1, \dots, V_k)$  be the coloring of  $G$ . The color class  $V_i$ , ( $1 \leq i \leq k$ ) is said to be the spare color class with respect to  $C$  if every vertex  $v \in V(G)$  dominates some color class  $V_j$ ,  $j \neq i$ , of  $C$ .

**Theorem 2.** [1] *Given a graph  $G$ ,  $\chi_d(\mu(G)) = \chi_d(G) + 1$  if and only if for some  $\chi_d$ -coloring  $C$  of  $G$ :*

- (i) *each vertex  $v$  dominates some color class  $V_i$  with  $v \notin V_i$ ;*
- (ii) *a vertex  $v$  is a solitary vertex and  $C$  contains a spare color class  $V_i$  which does not contain any vertex of  $N(v)$ .*

**Theorem 3.** [11] *The global dominator chromatic number of a complete  $m$ -partite graph is  $2m$ .*

**Theorem 4.** [11] *For any graph  $G$ , we have  $\chi_d(G) \leq \chi_{gd}(G) \leq 2\chi_d(G)$ .*

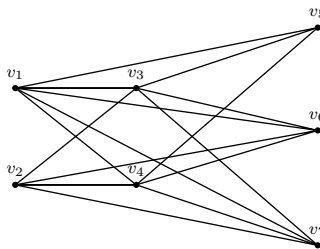
**Conjecture 1.** [11] *Let  $G$  be a graph with  $\Delta(G) < n - 1$ . Then  $\chi_{gd}(G) = 2\chi_d(G)$  if and only if  $G$  is a complete multipartite graph.*

Clearly if  $G$  is complete multipartite graph, then  $\chi_{gd}(G) = 2\chi_d(G)$  (by Theorem 3). In this paper, we give a counterexample to conclude the conjecture is false. i.e if  $\chi_{gd}(G) = 2\chi_d(G)$ , then the graph  $G$  need not be a complete multipartite graph. Also motivated by the works of Arumugam et al. [2], we establish the upper and lower bound for global dominator chromatic number of Mycielskian of the graph  $G$  in terms of dominator chromatic number of  $G$ .

## 2. Counterexample for the Conjecture 1

In this section we give a counterexample of a graph with  $\chi_{gd}(G) = 2\chi_d(G)$  which is not complete multipartite.

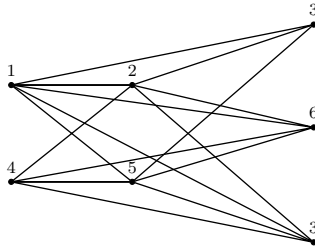
**Lemma 1.** *Let  $H$  be the graph in the Figure 1. Then  $\chi_d(H) = 3$  and  $\chi_{gd}(H) = 6$ .*



**Figure 1.** Graph  $H$

*Proof.* Since the graph  $H$  has  $K_3$  as the subgraph, minimum three colors are required for coloring of  $H$ . Hence  $\chi_d(H) \geq \chi(H) \geq 3$ . The coloring  $C = (\{v_1, v_2\}, \{v_3, v_4\}, \{v_5, v_6, v_7\})$  is a  $\chi_d$ -coloring of  $H$ . Hence,  $\chi_d(H) = 3$  and  $\chi(H) = 3$ . Since  $v_1v_3 \in E(G)$ ,  $v_1, v_3$  receive different colors. Now the color of  $v_1$  cannot be given to  $v_2$ , otherwise  $v_1$  will not have anti-dom color class. Similarly color of  $v_3$  cannot be given to  $v_4$ . Therefore  $v_1, v_2, v_3, v_4$  receive different colors in a global dominator coloring of  $G$ . Therefore  $\chi_{gd}(H) \geq 4$ . Now  $v_5$  cannot be given the color of  $v_2$ , otherwise  $v_5$  will not have anti-dom color class. Therefore  $v_5$  receive distinct color. Hence  $\chi_{gd}(H) \geq 5$ . If  $v_6, v_7$  receive the color of  $v_5$ , then  $v_6$  and  $v_7$  will not have anti-dom

color class. Therefore either  $v_6$  or  $v_7$  has to be given a new color. Hence  $\chi_{gd}(H) \geq 6$ . From the  $\chi_{gd}$  coloring of  $H$  in Figure 2, we can conclude that  $\chi_{gd}(H) = 6$ .  $\square$



**Figure 2.**  $\chi_{gd}$ -coloring of  $H$

From the Lemma 1, it is clear that  $\chi_{gd}(H) = 2\chi_d(H)$  but  $H$  is not a complete multipartite graph. Therefore if  $\chi_{gd}(G) = 2\chi_d(G)$ , then  $G$  need not be the complete multipartite graph. By the proof technique used in Lemma 1, we define a family of graphs  $G \in \mathfrak{S}$  which are not complete multipartite but satisfy  $\chi_{gd}(G) = 2\chi_d(G)$ . The graphs  $G \in \mathfrak{S}$  are constructed as follows,

- i)  $V_1, V_2, V_3$  are independent sets in  $G$  such that  $|V_i| \geq 2$ , for all  $1 \leq i \leq 3$ .
- ii) Let  $v_1 \in V_1$  and  $v_3 \in V_3$ . Join all the edges in  $G$  except  $v_1v_3$ .

**Corollary 1.** *If  $G \in \mathfrak{S}$ , then  $\chi_{gd}(G) = 2\chi_d(G)$ .*

Now we define a new family of graphs.  $G \in \mathfrak{S}_1$ , if for every  $\chi_d$ -coloring  $C = (V_1, \dots, V_k)$  of  $G$ , the following conditions are satisfied,

- i)  $|V_i| \geq 2$ , for all  $1 \leq i \leq k$  and
- ii) there exists atleast one vertex in each  $V_i$  that has at least one neighbor in each  $V_j$ , for  $j = 1, 2, \dots, k$  and  $i \neq j$ .

i.e in simple words,  $G$  is a  $k$ -partite graph with at least two vertices in each partite sets such that there exists at least one vertex in each partite set that has at least one neighbor in each of the other partite sets.

**Theorem 5.**  $\chi_{gd}(G) = 2\chi_d(G)$  if and only if  $G \in \mathfrak{S}_1$ .

*Proof.* Let  $G$  be a graph with  $\chi_d(G) = k$ . Suppose  $G \notin \mathfrak{S}_1$ .

**Case 1.** If there is a  $\chi_d$ -coloring  $C = (V_1, \dots, V_k)$  of  $G$  such that  $|V_i| = 1$ , for some  $1 \leq i \leq k$ . Let  $v_i \in V_i$ . the coloring  $C' = (V_j - \{v_j\}, V_i, \{v_j\})$  for  $j = 1, 2, \dots, k$  and  $i \neq j$  is a global dominator coloring of  $G$  with less than  $2\chi_d(G)$  number of colors. Note that  $v_i \in V_i$  cannot be adjacent to all the vertices of  $V_j \in C'$ , since  $G$  cannot have a vertex of degree  $n - 1$  for a global dominator coloring to exist.

**Case 2.** There is some  $\chi_d$ -coloring  $C = (V_1, \dots, V_k)$  such that every vertex in some  $V_i$  has no neighbor in some  $V_j$ . Therefore every vertex in  $V_i$  has an anti-dominator color class. Let  $v_i \in V_i$ , then the coloring  $C' = (V_j - \{v_j\}, V_i, \{v_j\})$  for  $j = 1, 2, \dots, k$  and  $i \neq j$  is a global dominator coloring of  $G$  with less than  $2\chi_d(G)$  number of colors. Conversely, suppose  $G \in \mathfrak{S}_1$ . Then for every  $\chi_d$ -coloring  $C = (V_1, \dots, V_k)$ , we have  $|V_i| \geq 2$  and there exists atleast one vertex  $v_i$  in each  $V_i$  that has atleast one neighbor in each  $V_j$ , for  $j = 1, \dots, k$  and  $i \neq j$ . Then the coloring  $C' = (V_i - \{v_i\}, \{v_i\})$  is a global dominator coloring of  $G$  with at least  $2\chi_d(G)$  number of colors. From Theorem 4, the proof follows.  $\square$

### 3. Bounds on Global dominator chromatic number of Mycielskian of a graph

For a graph  $G = (V, E)$ , the Mycielskian of  $G$  denoted by  $\mu(G)$  is the graph with vertex set  $V \cup V' \cup \{u\}$  where  $V' = \{x' \mid x \in V\}$  and is disjoint from  $V$ , and edge set  $E' = E \cup \{xy' \mid xy \in E\} \cup \{x'u \mid x' \in V'\}$ . The vertices  $x$  and  $x'$  are called twins of each other and  $u$  is called the root of  $\mu(G)$ . For results on domination parameters in Mycielskian of a graph, refer to [1, 4, 6]. In this section, we establish the upper and lower bound for global dominator chromatic number of Mycielskian of the graph  $G$  in terms of dominator chromatic number of  $G$ .

**Theorem 6.** *For any graph  $G$ , we have  $\chi_d(G) + 1 \leq \chi_{gd}(\mu(G)) \leq \chi_d(G) + 2$ .*

*Proof.* We know that  $\chi_{gd}(\mu(G)) \geq \chi_d(\mu(G))$  (by the Theorem 4 applied to  $\mu(G)$ ) and  $\chi_d(\mu(G)) \geq \chi_d(G) + 1$  (by the Theorem 1). So  $\chi_{gd}(\mu(G)) \geq \chi_d(G) + 1$ .

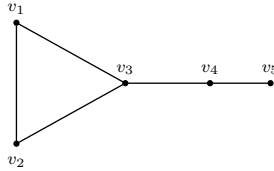
Let  $C = (V_1, V_2, \dots, V_{\chi_d})$  be the  $\chi_d$ -coloring of  $G$ . Now consider the graph  $\mu(G)$  and color the vertices of  $\mu(G)$  as follows,

- (i) color the vertices of  $G$  by the coloring  $C$  using  $\chi_d$  number of colors.
- (ii) color the vertices of  $V'$  by a unique new color.
- (iii) a new color to  $\{u\}$

In this coloring (say  $C'$ ), vertices of  $G$  have dom-color class as the coloring  $C$  is the  $\chi_d$ -coloring of  $G$  and have  $\{u\}$  as the anti-dom color class. The vertex  $u$  dominates the color class  $V'$  and anti-dominates all the color classes  $V_i$ . Now the vertices of  $V'_i$  dominates the color class  $\{u\}$  and anti dominates the color class  $V_i$  since no vertex of  $V'_i$  will be adjacent to any vertex of  $V_i$  by the construction of Mycielskian of  $G$ . So the coloring  $C'$  is the global dominator coloring of  $\mu(G)$  with at most  $\chi_d(G) + 2$  number of colors. Hence  $\chi_{gd}(\mu(G)) \leq \chi_d(G) + 2$ .  $\square$

**Lemma 2.** *Let  $G_1$  be the graph in the Figure 3. Then  $\chi_{gd}(\mu(G_1)) = \chi_d(G_1) + 1$ .*

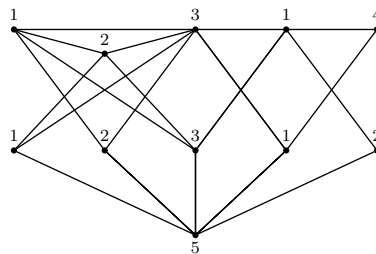
*Proof.* Consider the graph  $G_1$ . The vertices  $v_1, v_2$  and  $v_3$  have to be colored using three colors. The vertex  $v_4$  or  $v_5$  has to be given a new color in order to achieve the



**Figure 3.** Graph  $G_1$

$\chi_d$  as well as  $\chi_{gd}$ -coloring of  $G_1$ . So  $\chi_{gd}(G_1) = \chi_d(G_1) = 4$ .

Consider the global dominator coloring of  $\mu(G_1)$  as shown in the Figure 4.



**Figure 4.** Global dominator coloring of  $\mu(G_1)$

Therefore  $\chi_{gd}(\mu(G_1)) \leq 5$  and by the Theorem 6,  $\chi_{gd}(\mu(G_1)) \geq \chi_d(G_1) + 1 = 4 + 1$ . Hence  $\chi_{gd}(\mu(G_1)) = \chi_d(G_1) + 1$ . □

The graph  $G_1$  in Figure 3 with  $\chi_d$ -coloring  $C = (\{v_1, v_4\}, \{v_2\}, \{v_3\}, \{v_5\})$  satisfies the conditions of Theorem 7 with the vertex  $v_5$  being solitary and color class  $\{v_2\}$  being the spare color class. This example motivates us to state Theorem 7.

**Theorem 7.** Suppose for some  $\chi_d$ -coloring  $C$  of  $G$ , the following conditions are satisfied,

- i) a vertex  $v_1 \in G$  such that  $v_1$  is solitary.
- ii)  $C$  contains a spare color class  $V_i$  which does not contain any vertex of  $N(v_1)$ .
- iii) For all  $w \in N(v_1)$ ,  $w$  does not have neighbors in  $V_i$ .

Then  $\chi_{gd}(\mu(G)) = \chi_d(G) + 1$ .

*Proof.* Let  $C = (V_1, V_2, \dots, V_{\chi_d})$  be the  $\chi_d$ -coloring of  $G$ . Let the vertex  $v_1$  be solitary and the color class  $V_i$  (for some  $1 \leq i \leq \chi_d$ ) be the spare color class with respect to the coloring  $C$  such that  $V_i$  does not contain any vertex of  $N(v_1)$  and  $w$  has no neighbors in  $V_i$ , for all  $w \in N(v_1)$ . Consider the coloring  $C' = (C - V_i) \cup \{V_i \cup \{v'_1\}, \{u\}\}$  of  $\mu(G)$ , where each vertex  $v'_j$  ( $2 \leq j \leq \chi_d$ ) is given a color of vertex  $v_j$ ,  $v'_1$  is given the color of spare color class  $V_i$  and a new color is assigned to the vertex  $u$ . By the Theorem 2, coloring  $C'$  will be the dominator coloring of  $\mu(G)$ . The vertices of  $V(G)$  in  $\mu(G)$  anti dominates  $\{u\}$ , the vertex  $u$  anti dominates  $\{v_1\}$  and the vertices

of  $V'$  which are the twin vertices of non-neighbors of  $v_1$  anti dominates color class  $\{v_1\}$ . The condition that  $w$  does not have neighbors in  $V_i$ , for all  $w \in N(v_1)$  imply that the vertices of  $V'$  which are twins of neighbors of  $v_1$  anti dominates the spare color class  $V_i$ . Thus  $\chi_{gd}(\mu(G)) \leq \chi_d(G) + 1$  and the equality follows by the Theorem 6.  $\square$

**Theorem 8.** *Let  $G$  be the complete  $m$ -partite graph ( $m \geq 2$ ). Then  $\chi_{gd}(\mu(G)) = \chi_d(G) + 2$ .*

*Proof.* Let  $G$  be a complete  $m$ -partite graph with vertex set  $V$  and partite sets  $V_1, \dots, V_m$ . Since  $G$  is the complete  $m$ -partite graph,  $\chi_d(G) = m$  where each set  $V_i$  is given a unique color. Every vertex  $v_i \in V_i$  of  $G$  is adjacent to every other vertex of  $V_j$  ( $i \neq j$ ) and hence adjacent to every vertex of twins of  $V_j$  in  $\mu(G)$ .

**Case 1.** If the vertex  $u$  is given any one of color used in coloring  $G$ , then the vertices of  $V$  has to anti dominate a color class in  $V'$ . So at least  $m$  new colors will be required to color the vertices of  $V'$  since the vertex of  $V_i$  has to anti-dominate the color class  $V'_i$ . But  $m \geq 2$  imply that  $\chi_{gd}(\mu(G))$  is at least  $\chi_d(G) + 2$ .

**Case 2.** If  $\{u\}$  is given a new color, then the vertices of  $G$  in  $\mu(G)$  have  $\{u\}$  as the anti dom-color class. Now the only possibility of giving the colors used in coloring  $G$  to the vertices of  $V'$  is by giving the color of  $v \in V(G)$  to its twin vertex  $v' \in V'(G)$ . In that case the vertices of  $V'$  will not have anti dom-color class. Therefore a new unique color has to be given to vertices of  $V'$ . Then the vertex  $v'$  anti dominates the color class in which  $v$  lies.

From the above two cases, it is clear that at least  $\chi_d(G) + 2$  number of colors are required for global dominator coloring of  $\mu(G)$ . So by the Theorem 6, we have  $\chi_{gd}(\mu(G)) = \chi_d(G) + 2$ .  $\square$

## 4. Open problems

**Problem 1.** The graph  $G_1$  in Figure 3 is such that  $\chi_d(\mu(G_1)) = \chi_{gd}(\mu(G_1)) = \chi_d(G) + 1$ . This helps us to pose a question that for which graphs  $G$ ,  $\chi_d(\mu(G)) = \chi_{gd}(\mu(G))$ ?

**Problem 2.** Characterize graphs  $G$  such that  $\chi_{gd}(\mu(G)) = \chi_d(G) + 1$ .

**Problem 3.** Characterize graphs  $G$  such that  $\chi_{gd}(\mu(G)) = \chi_d(G) + 2$ .

**Problem 4.** Give a structural characterization for graphs  $G$  such that  $\chi_{gd}(\mu(G)) = 2\chi_d(G)$ .

**Problem 5.** The graphs  $G \in \mathfrak{S}$  in the Corollary 1 are graphs such that  $\chi_d(G) = 3$  and  $\chi_{gd}(G) = 6$ . One can attempt to construct graphs  $G$  such that  $\chi_d(G) = k$  and  $\chi_{gd}(G) = 2k$ , for all  $k \geq 4$ .

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**Conflict of interest.** The authors declare that they have no conflict of interest.

**Data Availability.** Data sharing is not applicable to this article as no datasets were generated or analyzed during the current study.

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